## 國立清華大學數學系訪問學者學術演講

## NTHU Department of Mathematics Visiting Scholar Colloquium

- 講者 張德健教授 (Georgetown University)
- 時間 2023.6.21 (Wed.) 10:30-11:30
- 地點 Lecture Room B, 4F, General Building III
- 茶會 10:00, Room 707, General Building III

## Abstract

The theory of singular integrals (SIO), introduced by Calderón and Zygmund as part of the theory of elliptic PDE's, has seen many extensions to different settings. Remaining within  $\mathbb{R}^n$  as the ambient space, the variations introduced involve the following aspects, possibly also combined together:

(a) replace the standard dilations, *i.e.*, scalar multiplications, with non-isotropic ones;

(b) distinguish between a "global" theory and a "local" one;

(c) allow multi-parameter dilations.

The basic property that is common to all these types of singular integral operators is  $L^p$ -boundedness for 1 and*failure* $of <math>L^p$ -boundedness, in general, for other values of p.

Hardy spaces  $H^p$  enter into this picture as the natural substitutes of  $L^p$  with  $0 , allowing positive results about <math>H^p \to H^p$  and  $H^p \to L^p$  boundedness of singular integrals for these values of p. The point is that each of the classes of SIO mentioned above admits its own Hardy spaces, so that, whenever a new class of SIO is introduced, it is natural to ask what are its Hardy spaces.

In this talk, I will use Kohn Laplacian on a family of model domains as an example to see how harmonic analysis, especially different type of singular integral operators arise.

\*歡迎參加,敬請張貼\* http://www.math.nthu.edu.tw